Nanoscale surficial films and a surface transition in V$_2$O$_5$–TiO$_2$-based ternary oxide systems

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Abstract

Nanoscale, vanadia-based, quasi-liquid films of self-selecting (equilibrium) thickness were observed on TiO$_2$ surfaces in six ternary oxide systems (Ti–V–X–O; X = P, Na, K, Nb, Mo or W). It is demonstrated that the film appearance and thickness could be tailored via co-doping or changing the equilibration temperature. Furthermore, the observed discontinuous changes in film thickness, hysteresis and bimodal thickness distributions indicate a first-order monolayer-to-multilayer adsorption transition, which is interpreted as a coupled prewetting and premelting transition. The film thickness and stability are measured as functions of equilibration temperature, anneal time, thermal treatment history, co-doping, overall composition and TiO$_2$ phase and orientation. The characterization of more than 850 independent films represents the most systematic measurement of similar interfacial films to date, providing insights into the formation mechanisms and the thermodynamic stability of equilibrium-thickness surficial films and analogous intergranular films.

Keywords: Wetting; Surface segregation; Phase transformation; Interfaces; Catalysis

1. Introduction

Nanoscale, impurity-based films of similar character have been widely observed at grain boundaries (GB) in ceramics [1–6] and metals [3,7,8], at hetero-interfaces in ceramic-ceramic [3] and metal–oxide [9–12] systems, and on free surfaces in oxides [11,13–17]. These films are called intergranular (glassy) films (IGF) or surficial amorphous films (SAF), although some partial structural order generally exists within them [3,13]. These surficial and intergranular films represent non-wetting conditions. Sufficient data are now available to interpret these IGF and SAF alternatively as equilibrium-thickness interfacial films [1,3,13,18,19] or multilayer adsorbates [2–6,13,16,19]. Nanometer-thick, impurity-based, quasi-liquid films can also be stabilized below the bulk solidus temperatures [3], where analogies to the simpler interfacial phenomena of premelting (in unary systems) [20] and prewetting (in binary de-mixed liquids) [21] can be made. Further discussions of these related interfacial phenomena and terms/jargon can be found in recent reviews [3,13].

Recently, Tang et al. [22] proposed that subsolidus IGF can be understood as quasi-liquid interfacial films formed from coupled GB prewetting and premelting transitions in a diffuse-interface model, and these GB transitions can be first order. A similar theory has also been proposed for SAF [19]. Furthermore, Dillon et al. observed several disordered GB structures (complexions) in doped Al$_2$O$_3$, implying the existence of GB transitions between them [5,6]. Yet, first-order transitions from monolayer/sub-monolayer adsorption to nanoscale quasi-liquid films have not been directly observed at surfaces or GB in ceramics. In addition to their scientific significance, GB and surface transitions are of practical importance because they cause abrupt changes in transport kinetics [5,6] and material properties [3]. Consequently, this study sought a surface transition in V$_2$O$_5$–TiO$_2$-based systems.
Titania-supported vanadia (V₂O₅/TiO₂) catalysts are widely used for partial oxidation and ammoxidation of alkylationaromatic compounds and selective catalytic reduction of NOₓ [23–28]. Furthermore, V₂O₅/TiO₂ is a model system for a broad class of “monolayer catalysts”, including MoO₃/Al₂O₃, Cr₂O₃/Al₂O₃, WO₃/Al₂O₃, Re₂O₇/Al₂O₃, TiO₂/SiO₂, Fe₃O₅/SiO₂, NiO/ZrO₂ and WO₃/ZrO₂ [23,25,29]. It is generally believed that monolayer surface adsorption of the catalytic oxide species on refractory oxide supports occurs during calcination (isothermal annealing) in these systems. This thermal spreading occurs at ~350–450 °C for V₂O₅/TiO₂ [24,25]. However, nanoscale, amorphous films are occasionally observed in V₂O₅/TiO₂, and the thickness of these films is assumed to be supply controlled [27,28]. It is further suggested that these amorphous films form owing to an unknown impurity effect [24]. A recent letter [17] reported the stabilization of nanoscale quasi-liquid films for V₂O₅ on TiO₂ anatase (101) facets at moderate (yet subeutectic) temperatures of ~550–600 °C, using purer (99.7+%) anatase powder (as opposed to the ~99% pure pigment grade powders used in the prior study [28] and in industry). Upon achieving thermodynamic equilibrium, these surficial films exhibit an equilibrium thickness independent of synthesis routes, annealing time and the amount of excess secondary phases [17]. In the present study, the impurity effects (using 99.99% anatase powder plus controlled co-doping) and the films formed on different facets and curved surfaces were further investigated. Moreover, the concept of controlling the film appearance and thickness thermodynamically via co-doping or temperature was exploited, which is of practical importance in tailoring supported oxide catalysts and controlling SAF of self-selecting thickness for other applications (e.g., device junctions or morphological control of nanocrystals) [13].

This study was further motivated by the critical need to develop a systematic dataset to probe the formation mechanisms of SAF and analogous IGF. Nanometer-thick IGF, ubiquitous in structural ceramics, thick-film resistors, varistors, high Tc superconductors and refractory metals, are known to play important roles in sintering and grain growth, and in the mechanical and physical properties of these materials (see, e.g., a recent review article [3] and references therein). However, the much needed systematic measurements of temperature- and composition-dependent IGF stability are lacking owing to the low efficiency of TEM specimen preparation and the complexity of controlling GB crystallography, whereas systematic measurements of analogous SAF on a fixed surface orientation are feasible via a more efficient powder experiment [13]. Such measurements can reveal the SAF formation mechanism, which is of critical importance; furthermore, they can provide insights into the understanding of parallel IGF, for which collecting large amounts of data is difficult. In addition, because V₂O₅/TiO₂ particles are relatively stable against coarsening, SAF are observed more frequently in V₂O₅/TiO₂ than in the Bi₂O₃/ZnO model system [13,15,16]. This permits even more systematic measurements of the film appearance and thickness as a function of various experimental parameters. These measurements were then used to test key hypotheses on the thermodynamic stability and formation mechanisms of SAF and analogous IGF, which was the purpose of this study.

2. Experimental procedure and data analysis

TiO₂ anatase particles (5–15 nm, 99.99%, the purest nano-sized anatase particles commercially available) were purchased from MTI Corporation (Richmond, CA) and annealed at 250 °C for 4 h to remove moisture. Nano-sized rutile particles were purchased from Sigma-Aldrich. Ammonium vanadate precursor (NH₄VO₃, 99.995%) was purchased from Alfa Aesar. Mixtures of TiO₂ particles and vanadate precursor were prepared by incipient wetness impregnation in aqueous solutions [28]. The mixtures were dried at 85 °C overnight, and an additional cycle of wet impregnation and drying was used to add co-dopants. Here, a co-dopant is defined as a cationic additive other than Ti and V. Co-dopants of Mo, W, Nb, K, Na and P were introduced via using the following precursors: (NH₄)₂MoO₄ (99.997%; Alfa Aesar), (NH₄)₂WO₄ (99.99%+; Alfa Aesar), Nb(HC₂O₄)₅·6H₂O (Alfa Aesar), K₂CO₃ (99.995%+; ACROS), Na₂CO₃ (99.98+%; Fisher), and H₂PO₄ (99.95%; Alfa Aesar). The dried specimens were annealed at 220 °C for 3 h and calcined at 450 °C (or 350 °C for selected P co-doped specimens to reduce P₂O₅ evaporation) for 3 h in open containers to form binary or ternary oxides (although a small fraction of carbonates was expected to remain in the specimens that were co-doped with Na and K). Finally, the oxide mixtures were isothermally annealed at the desired equilibration temperatures in closed containers and then air quenched. Specimens were isothermally annealed at each desired temperature for 4 h unless otherwise noted.

X-ray diffraction (XRD) experiments were carried out using a Scintag 2000 diffractometer (Cu Kα radiation, λ = 1.5418 Å, operating at 40 kV and 35 mA). High-resolution transmission electron microscopy (HRTEM) specimens were prepared by dispersing particles ultrasonically in acetone and placing a small amount of suspension onto carbon-coated Cu grids. The specimens were then dried overnight in a desiccator. Particle surfaces were characterized using a Hitachi 9500 microscope (300 kV, LaB₆ source, 0.10 nm lattice resolution and 0.18 nm point-to-point resolution). Minimum exposure was used during HRTEM to avoid electron beam damage. For statistical analysis, images of randomly selected particle surfaces were recorded. Scale bars were calibrated prior to measurements of film thickness.

To ensure that specimens had the proper “edge-on” conditions to measure film thickness accurately, for films on (101) or (001) facets, HRTEM images were used only if the parallel (101) or (001) fringes were clearly imaged so that the electron beam was parallel to the surfaces, thus
ensuring that the corresponding errors in thickness measurements were small. For films on curved surfaces, such errors are generally insignificant. Furthermore, these errors in measured thicknesses should be no greater than the typical surface-to-surface variations in measured film thicknesses. The standard deviations of measured thicknesses were ~0.15 nm for films without co-doping (Table 1), being close the point-to-point resolution of the microscope (0.18 nm). Thus, the effects of misalignment on film thickness measurements were relatively insignificant.

To measure the film thickness, two lines were drawn to represent the dividing planes for the crystal–film and film–vapor interfaces, respectively. Examples are shown in Fig. 1. When small crystallites or partial order were observed within the film, the dividing line for the crystal–film interface was assumed to be the outmost continuous line in the crystal (thus the small crystallites were in the film). An example is shown in Fig. 1b.

The measured film thicknesses were averaged twice for each specimen. First, film thickness was measured at every 4 nm along the surface for each independent SAF. The mean of these measurements represents the thickness of one independent SAF, and the corresponding standard deviation (σ) represents a surface-to-surface variation in the thickness of films on different particle surfaces in one specimen. In Table 1, n

### Table 1

Summary of measurements of SAF in V$_2$O$_5$–TiO$_2$-based systems

<table>
<thead>
<tr>
<th>Specimens</th>
<th>(101) facets</th>
<th>Curved</th>
<th>(001) facets</th>
<th>Notes</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>μ ± σ (nm)</td>
<td>n ± (n)</td>
<td>μ ± σ (nm)</td>
<td>n ± (n)</td>
</tr>
<tr>
<td>(1.2–14.7)Ti:1V, 600 °C (2–24 h)</td>
<td>1.11 ± 0.25</td>
<td>109</td>
<td>0.55 ± 0.08</td>
<td>9</td>
</tr>
<tr>
<td>5.2Ti:1V, 600 °C</td>
<td>0.97 ± 0.21</td>
<td>7</td>
<td>0.72 ± 0.17</td>
<td>9</td>
</tr>
<tr>
<td>5.2Ti:1V, 575 °C</td>
<td>0.78 ± 0.13</td>
<td>8</td>
<td>0.64 ± 0.06</td>
<td>7</td>
</tr>
<tr>
<td>5.2Ti:1V, 550 °C</td>
<td>0.71 ± 0.12</td>
<td>5</td>
<td>0.61 ± 0.06</td>
<td>7</td>
</tr>
<tr>
<td>5.2Ti:1V, 500 °C</td>
<td>0.00 (6)</td>
<td></td>
<td>0.72 ± 0.17</td>
<td>7</td>
</tr>
<tr>
<td>5.2Ti:1V, 600 °C + 550 °C</td>
<td>0.56 ± 0.09</td>
<td>7</td>
<td>0.76 ± 0.10</td>
<td>7</td>
</tr>
<tr>
<td>5.2Ti:1V, 600 °C + 500 °C</td>
<td>0.47 ± 0.06</td>
<td>7</td>
<td>0.35 ± 0.08</td>
<td>7</td>
</tr>
<tr>
<td>5.2Ti:1V,600 °C + 450 °C</td>
<td>0.00 (8)</td>
<td></td>
<td>0.00 (8)</td>
<td></td>
</tr>
<tr>
<td>3.1Ti:1V, 600 °C</td>
<td>0.94 ± 0.12</td>
<td>18</td>
<td>0.69 ± 0.12</td>
<td>11</td>
</tr>
<tr>
<td>5.2Ti:1V, 600 °C</td>
<td>0.97 ± 0.15</td>
<td>56</td>
<td>0.79 ± 0.20</td>
<td>29</td>
</tr>
<tr>
<td>8.1Ti:1V, 600 °C</td>
<td>0.92 ± 0.21</td>
<td>10</td>
<td>0.76 ± 0.10</td>
<td>10</td>
</tr>
<tr>
<td>14.6Ti:1V, 600 °C</td>
<td>0.61 ± 0.12</td>
<td>15</td>
<td>0.72 ± 0.07</td>
<td>15</td>
</tr>
<tr>
<td>5.2Ti:1V, 600 °C (2 h)</td>
<td>0.82 ± 0.10</td>
<td>7</td>
<td>0.89 ± 0.09</td>
<td>7</td>
</tr>
<tr>
<td>5.2Ti:1V, 550 °C</td>
<td>0.63 ± 0.06</td>
<td>10</td>
<td>0.55 ± 0.08</td>
<td>9</td>
</tr>
<tr>
<td>5.2Ti:1V0.07P, 600 °C</td>
<td>0.94 ± 0.22</td>
<td>32</td>
<td>0.80 ± 0.16</td>
<td>8</td>
</tr>
<tr>
<td>5.2Ti:1V0.1P, 600 °C</td>
<td>1.10 ± 0.21</td>
<td>123</td>
<td>1.05 ± 0.31</td>
<td>24</td>
</tr>
<tr>
<td>5.2Ti:1V0.2P, 600 °C</td>
<td>1.22 ± 0.34</td>
<td>42</td>
<td>1.14 ± 0.18</td>
<td>5</td>
</tr>
<tr>
<td>5.2Ti:1V0.4P, 600 °C</td>
<td>0.97 ± 0.16</td>
<td>20</td>
<td>1.00 ± 0.17</td>
<td>9</td>
</tr>
<tr>
<td>5.2Ti:1V1P, 600 °C</td>
<td>1.15 ± 0.23</td>
<td>17</td>
<td>0.92 ± 0.09</td>
<td>7</td>
</tr>
<tr>
<td>9.2Ti:1V0.1P, 550 °C</td>
<td>0.99 ± 0.21</td>
<td>12</td>
<td>0.92 ± 0.09</td>
<td>2</td>
</tr>
<tr>
<td>5.2Ti:1V0.1P, 550 °C</td>
<td>1.20 ± 0.31</td>
<td>19</td>
<td>1.35 ± 0.33</td>
<td>6</td>
</tr>
<tr>
<td>5.2Ti:1V0.1P, 525 °C</td>
<td>0.93 ± 0.13</td>
<td>5</td>
<td>1.10 ± 0.14</td>
<td>5</td>
</tr>
<tr>
<td>5.2Ti:1V0.1P, 500 °C</td>
<td>0.00 (7)</td>
<td>0.00 (5)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>5.2Ti:1V0.1P, 550 °C + 500 °C</td>
<td>0.95 ± 0.20</td>
<td>11</td>
<td>1.31 ± 0.37</td>
<td>2</td>
</tr>
<tr>
<td>5.2Ti:1V0.1P, 550 °C + 450 °C</td>
<td>0.45 ± 0.30</td>
<td>20 (4)</td>
<td>0.47 ± 0.09</td>
<td>9</td>
</tr>
<tr>
<td>5.2Ti:1V0.1P, 550 °C + 450 °C (24 h)</td>
<td>~0.00 (1)</td>
<td>1 (25)</td>
<td>0.00</td>
<td></td>
</tr>
<tr>
<td>5.2Ti:1V0.1P, 550 °C + 400 °C</td>
<td>0.16 ± 0.25</td>
<td>9 (20)</td>
<td>0.00</td>
<td>0.00 (3)</td>
</tr>
<tr>
<td>5.2Ti:1V0.1Na, 600 °C</td>
<td>1.00 ± 0.14</td>
<td>14</td>
<td>1.14</td>
<td>1</td>
</tr>
<tr>
<td>5.2Ti:1V0.1K, 600 °C</td>
<td>0.99 ± 0.08</td>
<td>14</td>
<td></td>
<td></td>
</tr>
<tr>
<td>5.2Ti:1V0.1Mo, 600 °C</td>
<td>0.76 ± 0.15</td>
<td>16</td>
<td>0.53</td>
<td>1</td>
</tr>
<tr>
<td>5.2Ti:1V0.2Mo, 600 °C</td>
<td>0.62 ± 0.10</td>
<td>24</td>
<td></td>
<td></td>
</tr>
<tr>
<td>5.2Ti:1V1W, 600 °C</td>
<td>0.76 ± 0.10</td>
<td>32</td>
<td>0.84 ± 0.21</td>
<td>6</td>
</tr>
<tr>
<td>5.2Ti:1V12W, 600 °C</td>
<td>0.61 ± 0.06</td>
<td>18</td>
<td></td>
<td></td>
</tr>
<tr>
<td>5.2Ti:1V0.2W, 600 °C</td>
<td>0.55 ± 0.08</td>
<td>9</td>
<td></td>
<td></td>
</tr>
<tr>
<td>5.2Ti:1V1W, 600 °C</td>
<td>0.64 ± 0.17</td>
<td>20</td>
<td></td>
<td></td>
</tr>
<tr>
<td>5.2Ti:1V0.1Nb, 600 °C</td>
<td>0.82 ± 0.13</td>
<td>13</td>
<td></td>
<td></td>
</tr>
<tr>
<td>5.2Ti:1V0.2Nb, 600 °C</td>
<td>0.72 ± 0.17</td>
<td>8</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Here, μ and σ are the mean and the standard deviation, respectively, of the thicknesses of measured films, n is the number of independent films observed, and n2 is the number of surfaces that are devoid of films. Anneal time was 4 h at each temperature unless otherwise noted in parentheses. For curved surfaces, surfaces that are devoid of films are not included for computing μ and σ, except that the thicknesses were noted as zero if no films were found.

a Data reported in Ref. [17]. These specimens were prepared using 99.7% pure anatase powder (whereas all other specimens were prepared using 99.99% pure anatase powder).

b This set of data includes 15 different specimens prepared using different synthesis routes, overall nominal compositions, and annealing times. But all these 15 specimens represent V$_2$O$_5$-saturated specimens equilibrated at 600 °C [17].

c Film thicknesses may be limited kinetically.
represents the number of independent SAF (each on a different particle surface). Approximately 1000 separate particle surfaces (including both independent SAF and surfaces without films) were characterized, and >3000 individual thickness measurements were made. Ninety-five percent confidence intervals were calculated from the standard deviations (σ) and the numbers of independent SAF (n).

Specimens were designated by the cationic ratios and normalized to 1 V. For example, “5.2Ti:1V:0.1P” represents a composition of “5.2TiO2 : 1/2V2O5 : (0.1 × 1/2)P2O5” or “TiO2 + 8.7 mol.% V2O5 + 0.87 mol.% P2O5”. These compositions are nominal overall compositions of the specimens (not film compositions).

3. Results and discussion

3.1. Vanadia-based surficial films on anatase: film characteristics

Nanoscale, vanadia-based SAF have been observed to form on more than 850 anatase particle surfaces in the V2O5–TiO2 binary system and in six V2O5–TiO2-based ternary oxides (Table 1). Representative HRTEM images of two surficial films formed at 600 °C on anatase (101) facets are shown in Fig. 1. Though these films exhibited a large degree of structural disorder (Fig. 1a), partial or local order was often seen in HRTEM. In particular, growth of small epitaxial clusters was occasionally observed. An example is shown in Fig. 1b. These small crystallites often formed in a periodic array, which was probably due to a strain effect. It was also presumed that these crystallites had (largely) formed during cooling. Both diffuse-interface theories [1,22] and molecular dynamics modeling [30] suggest the existence of partial structural order within the films. However, partial order probably intensified during quenching, and some observed order might be due to HRTEM delocalization effects.

These SAF, uniform in thickness along the surface (Fig. 1), had measured thicknesses that varied little from surface to surface for a fixed set of equilibrium conditions. For example, the mean thickness of 56 independent films in a 5.2Ti:1V specimen annealed at 600 °C for 4 h was 0.97 nm, and the corresponding standard deviation (σ) of 0.15 nm described a surface-to-surface variation. Furthermore, each of these 56 measured mean thicknesses represented an average of three to seven measurements at different locations along the film. The average film uniformity was represented by σu, the average of 56 individual σu (i.e., the standard deviation of measurements at different locations along one surface). This average film uniformity σu was 0.09 nm, which was lower than the surface-to-surface variation (σ) of 0.15 nm. A Gaussian-like distribution of all individual thickness measurements is shown in Fig. 2a. On average, the measured σu was about ~60% of the measured σ. Since some measured surface-to-surface variations in thickness may have resulted from misalignment and HRTEM imaging artifacts, the actual thickness distributions were probably tighter.

At a fixed equilibration temperature, V2O5-saturated specimens exhibited a constant thickness independent of the fraction of the V2O5 secondary phase (in the two-phase region with a constant V2O5 activity) once a thermodynamic equilibrium state was achieved. For example, for the nominal Ti/V ratios of 3.1, 5.2 and 8.1, the average measured film thicknesses were 0.94 nm, 0.97 nm and 0.92 nm, respectively, in specimens equilibrated at 600 °C.
for 4 h (Fig. 2c). In contrast, a supply-controlled thickness, as assumed in prior studies [27,28], should strongly correlate with the overall Ti/V ratio. Consequently, this study, in which a purer anatase powder was used, confirmed the existence of equilibrium thickness [17].

The equilibrium surficial films in unsaturated specimens with V₂O₅ contents below the solid solubility limit were expected to be thinner, akin to what has been observed for Bi₂O₃-enriched surficial films on ZnO [15,16]. However, in Fig. 2c, the 14.6Ti:1V specimen probably represented a V₂O₅-saturated specimen [31], where the thickness was presumably limited by slow transport kinetics. Similarly, the films were thinner in a specimen with a shorter anneal time of 2 h (Table 1), which was also probably an effect of kinetic limitation to equilibration.

3.2. Films on surfaces of different orientations or TiO₂ phases

It is known that (101) planes are the dominant (lowest-energy) facets for anatase crystals in the Wulff shape, and (001) planes are the only other facets that are present at equilibrium [32]. The present study further confirmed that the Wulff shape for V₂O₅-doped TiO₂ anatase particles is similar. Nanoscale SAF were found on virtually all (101) facets in specimens equilibrated at temperatures of 525 °C or higher (Fig. 1; Table 1). Similar films were also observed on several (001) facets and on more than 50% of curved surfaces (Fig. 3a). For a 5.2Ti:1V specimen annealed at 600 °C for 4 h, the average measured thickness of films formed on (101) facets, (001) facets, and curved surfaces were 0.97 nm, 0.89 nm and 0.79 nm, respectively (Fig. 3b). In general, (001) facets were not frequently observed.

Vanadia-based SAF of similar character were also observed on a fraction of the surfaces in V₂O₅/rutile specimens. Measurements of five SAF on rutile (110) facets in a 5.2Ti:1V specimen annealed at 600 °C for 4 h yielded a mean thickness of 0.87 nm with a standard deviation of 0.18 nm. One SAF that was approximately 0.95 nm thick was also found on a curved rutile surface in the same specimen. This study then focused on films on anatase (101) facets and curved surfaces, which were frequently observed.

3.3. Tailoring nanoscale surficial films via co-doping

Fig. 4 shows representative HRTEM images of SAF formed on anatase (101) facets at 600 °C in 5.2Ti:1V:0.1X (X = P, Na, K, Nb, Mo or W) specimens. Small additions of co-dopants changed the film thicknesses. As shown in Fig. 5a, minor additions of the oxides of Mo, W or Nb decreased the equilibrium thickness, and films were thinner for a larger X/V ratio (0.2 vs 0.1), whereas, the addition of P increased the film thickness appreciably. The addition of K or Na had no significant effect on thickness.

The film thickness vs W/V (or P/V) ratio is shown in Fig. 5b. The film thickness initially decreased (or increased) with increasing W (or P) co-doping level, and leveled off.
beyond a threshold. These observations may be explained on the same basis used to explain Fig. 2c. When a relatively large amount of W (or P) was added, WO$_3$ (or an unknown P-enriched oxide that gave XRD peaks at 2$\theta$ = 24.4 and 26.9) precipitated, and the W (or P) activity leveled off. The corresponding extra XRD peaks were observable at a W/V (or P/V) ratio of ~0.1–0.2, and their intensities increased significantly when this ratio was increased to 1. This observation was consistent with the concept that equilibrium thickness depends on the chemical potential rather than on the fraction of a secondary phase.

Furthermore, co-doping also changed the thickness distribution and film appearance. As shown in Fig. 2a and Fig. 2b, adding a small amount of P (~0.87 mol.% P or a P/V ratio of 0.1) increased the average film thickness appreciably and broadened the thickness distribution. The standard deviation was approximately doubled. A comparison of film thickness variability in Fig. 2a vs Fig. 2b indicates shallow vs deep minima in corresponding free energy vs thickness curves, although the exact physical origin of this difference is unknown. Co-doping with P reduced the differences between the average thicknesses of films formed on different facets and curved surfaces (Fig. 3b). The percentage of curved surfaces covered by nanoscale SAF was ~55% for a 5.2Ti:1V specimen equilibrated at 600 °C, which increased to ~90% and >95% with the addition of 0.87 mol.% P and ~1.7 mol.% P, respectively, as shown in Fig. 6. Thus, co-doping with P resulted in thicker and more isotropic SAF, although it broadened the thickness distribution at a fixed orientation.
Determining the effects of co-doping is important for tailoring supported oxide catalysts, as industrial catalysts typically contain additives or impurities [23–28]. Tuning IGF thickness via co-doping has been reported in Si$_3$N$_4$–SiO$_2$-based structural ceramics with Ca [33] or rare earth [34] additives and in Pb$_2$RuO$_7$–SiO$_2$-based, thick-film resistors with TiO$_2$ additives [35]. The present study further demonstrates the concept of tailoring average SAF thickness, thickness distribution, surface coverage and anisotropy via changing the bulk chemical potentials. These observations, which support the basic theory of equilibrium-thickness SAF (and IGF), provide comprehensive data for testing thermodynamic models.

3.4. Temperature dependence of film thickness: hysteresis and bimodal distributions

The thicknesses of films formed on anatase (101) facets and curved surfaces depend on temperature, as shown in Fig. 7. To probe the kinetic limitation to equilibration, specimens were allowed to approach their equilibrium states from both lower and higher temperatures. In the first instance, 5.2Ti:1V:0.1P specimens were directly heated to the desired temperature and equilibrated for 4 h. In the second instance, specimens were annealed at 550 °C for 4 h, to elicit conditions that could form ~1.2 nm thick films [on (101) facets] or ~1.35 nm thick films (on curved surfaces). The temperature was then reduced to the equilibration temperature at which the specimens were annealed for another 4 h. At relatively low temperature ranges (~350–450 °C) in which nanoscale surficial films are not discernible by HRTEM, monolayer (or submonolayer) adsorption is known to occur based on extensive prior studies [24,25].

Upon heating, discontinuous transitions were observed from submonolayer to multilayer coverage between 500 °C and 525 °C on both (101) facets and curved surfaces (Fig. 7). Upon cooling, the transition back to submonolayer coverage occurred at somewhat lower temperatures. The transition in 5.2Ti:1V:0.1P specimens was more abrupt than that observed in the V$_2$O$_5$–TiO$_2$ binary system [17]. In Fig. 7a, the reported film thicknesses for specimens in which the equilibration was approached from a higher temperature (as indicated by a solid line) represent the overall average thicknesses of two groups of films (as indicated by the dotted lines).

When the equilibration was approached from a higher temperature, bimodal thickness distributions for the SAF on anatase (101) facets were observed at 400 °C and 450 °C (Fig. 8a). In a 5.2Ti:1V:0.1P specimen annealed at 550 °C × 4 h+450 °C × 4 h, SAF were observed in 16 of 20 facets (80%) of (101) orientation with an average thickness of 0.57 nm, with four (101) facets (20%) devoid of discernible films (dried). With a reduction in temperature, among 29 (101) facets examined in a specimen annealed at 550 °C × 4 h+400 °C × 4 h, SAF were found on nine facets (31%) with an average thickness of 0.55 nm, with 20 facets (69%) dried. Furthermore, an increase in the equilibration time to 24 h at 450 °C (550 °C × 4 h+450 °C × 24 h) showed that 25 of 26 (101) facets (or ~96%) were dried (Fig. 8a). A representative HRTEM image of these dried surfaces is shown in Fig. 8b.

Nanoscale SAF were observed on all (101) facets in specimens equilibrated at 525 °C and higher temperatures, as well as in one specimen fired at 550 °C × 4 h+500 °C × 4 h. As SAF only formed on a fraction of curved surfaces, the data in Fig. 7b exclude surfaces devoid of films, but the
thickness is plotted as zero in cases where no SAF were found.

These observed discontinuous changes in thickness, hysteresis and bimodal thickness distributions suggest a first-order surface adsorption transition, which will be discussed further in Section 3.7.

3.5. Films coexisting with nano-drops: an analogy to frustrated-complete wetting

Whereas nanometer-thick SAF were found to coexist with nanoscale partial-wetting glassy droplets (Fig. 9) in the same set of specimens, they were found only in a small fraction of surfaces. Similar nanoscale wetting configurations have been previously reported for Bi$_2$O$_3$ on ZnO and MoO$_3$ on Al$_2$O$_3$ [16]. Here, phenomenological similarities to frustrated-complete wetting [36] and pseudo-partial wetting [37,38], proposed and confirmed for molecular substances and metallic systems, clearly exist. A discussion of these analogous wetting phenomena is in Ref. [3]. Although the cooling effects are unknown, Fig. 9 indicates that the excess glassy phase did not completely wet the surfaces; thus, these surficial films exhibited a self-limiting (equilibrium) thickness.
3.6. Film stability in a phenomenological model

In a phenomenological model [13], the excess free energy of an SAF of thickness $h$ is given by
\[ G_x(h) = c_{cl} + c_{lv} + \frac{D_G_{vol}}{C_1} h + r_{\text{interfacial}}(h) \]
where $c_{cl} + c_{lv}$ is the sum of crystal–liquid and liquid–vapor interfacial energies. The term $D_G_{vol}$ is the volumetric free energy for forming a hypothesized uniform liquid film from a mixture of bulk phases:
\[ D_G_{vol} = \frac{G_{f_{\text{liquid}}}}{C_0} X_i l_i \]
where $G_{f_{\text{liquid}}}$ is the liquid formation free energy, $X_i$ is the average fraction of the $i$th component in the film, $l_i$ is the chemical potential of the $i$th component set by the (equilibrium or metastable) bulk phases, and $\rho$ is density. This volumetric free energy is positive for quasi-liquid films equilibrated at subsolidus temperatures, and it can be evaluated via computational thermodynamics if relevant thermodynamic functions are known [39]. The $D_G_{vol} \cdot h$ term is generally the dominant attractive interaction in subsolidus regions that limits the film thickness [13]. Eq. (2) also implies that film thickness should depend on the chemical potentials of the bulk phases rather than the nominal overall composition or the fraction of a secondary phase, as shown in Figs. 2c and 5b.

When the film is thin, an extra interfacial free energy term $\sigma_{\text{interfacial}}(h)$ arises, representing the total contribution of all interfacial forces [13]. For SAF in oxides, this term can be expressed as
\[ \sigma_{\text{interfacial}}(h) = \frac{A_{123}}{12\pi h^2} + \sigma_{\text{short-range}}(h) + \sigma_{\text{elec}}(h) + \cdots \]

The first term is a long-range London dispersion interaction. The Hamaker constant $A_{123}$ was estimated for the $V_2O_5$ on anatase system from the optical and static dielectric constants of anatase ($n = 2.57$, $\varepsilon \approx 86$) [40] and $V_2O_5$ ($n = 1.97-2.12$, $\varepsilon \approx 20.1-37.2$, depending on orientation) [41] to be between $-88$ zJ and $-106$ zJ [42]. While this newer assessment will replace the prior inaccurate estimation [17], a more accurate calculation of $A_{123}$ should use a full-spectrum method [43] and consider the exact V valence states and film structure (which are currently unknown). Nonetheless, this estimation suggests that the dispersion force favors complete wetting. Thus, the film thickness is probably limited by the $D_G_{vol} \cdot h$ term at the subsolidus regime (Fig. 10) [13,15]. In Eq. (3), $\sigma_{\text{short-range}}(h)$
is a coupled short-range interaction of structural and chemical origins, and $r_{elec}(h)$ is an electrostatic interaction. By selecting the state of $h = +1$ as a reference state, the free energy terms that represent interfacial forces (i.e., $r_{vdW}(h)$, $r_{short-range}(h)$, $r_{elec}(h)$, etc., but not $\Delta G_{vol} \cdot h$) can be consistently defined so that they all vanish as $h \to +\infty$.

The excess film free energy, referred to the chemical potentials set by the bulk phases and the state of $h = 0$, is given by

$$\Delta \sigma(h) \equiv G(h) - \gamma_{cv}^{(0)} = \Delta \gamma^{(0)} + \Delta G_{vol} \cdot h + \frac{A_{123}}{12\pi h^2} + \sigma_{short-range}(h) + \cdots$$

Here, $\Delta \gamma^{(0)} \equiv (\gamma_{vl} + \gamma_{cl} - \gamma_{cv}^{(0)})$, where $\gamma_{cv}^{(0)}$ is the excess free energy of a “clean” surface without any adsorption (which differs from the true equilibrium $\gamma_{cv}$ that corresponds to the global minimum in Eq. (1)). Eq. (4) is a free-surface counterpart to the Clarke model for IGF [1,18], and can be considered a high-temperature colloidal theory with an additional $\Delta G_{vol} \cdot h$ term. An “equilibrium” thickness corresponds to a global or local minimum in excess film free energy vs thickness, which is defined by:

$$\frac{d[\Delta \sigma(h)]}{dh} \bigg|_{h=h_{eq}} = 0$$  

These quasi-liquid surficial films probably formed at subsolidus temperatures [17,31]. A prior study, reporting a eutectic reaction in the TiO$_2$–V$_2$O$_5$ binary system (producing V$_2$O$_5$ and rutile) at $\sim$631 °C [31], also suggests that a V$_2$O$_5$-induced anatase-to-rutile transition starts at $\sim$525 °C. However, XRD analysis showed a stability of the nano-sized anatase phase in these systems for annealing up to 600 °C, in which only a minor fraction of rutile phase formed. A subsolidus quasi-liquid SAF is thermodynamically stable if $\Delta \sigma(h) < 0$, an approximated condition for which is

$$\Delta G_{vol} \cdot h < [\gamma_{cv}^{(0)} - (\gamma_{vl} + \gamma_{cl})]$$

Stabilization of subsolidus quasi-liquid SAF in these binary and ternary systems has phenomenological similarities to the phenomenon of premelting in unary systems [20].

Fig. 8. (a) Evolution of bimodal distributions of measured film thicknesses for SAF formed on anatase (101) facets when equilibration was approached from a higher temperature. Each bar represents a measured thickness of an independent film on a separate particle surface. (b) A representative HRTEM image of a dried (101) facet in a 5.2Ti:V:0.1P specimen annealed at 550 °C × 4 h + 400 °C × 4 h. See text for details.
Eq. (6) illustrates that this stabilization can be conceived as if the free energy penalty for forming an undercooled liquid film is more than offset by the reduction of total interfacial energy resulting from the replacement of a high-energy “clean” crystal surface with a liquid surface and a crystal–liquid interface. In an alternative (and equivalent) approach, Eq. (6) can be rewritten as

\[ \Delta \sigma(h) = \Delta \gamma^{(0)} \cdot f(h) + \Delta G_{\text{vol}} \cdot h \]  

where the interfacial coefficient \( f(h) \) ranges from 0 to 1 as \( h \) increases from 0 to \( \infty \). The \( f(h) \) term can have multiple minima [44,45], leading to complex adsorption and wetting phenomena.

### 3.7. A first-order transition?

The observations of bimodal thickness distributions and their evolution (Fig. 8) indicate the existence of a global minimum (corresponding to monolayer or submonolayer adsorption) and a metastable minimum (corresponding to \( \approx 0.55 \) nm thick SAF) in excess free energy vs film thickness at 450 °C and 400 °C (Fig. 10). At higher temperatures, the global minimum is associated with nanoscale SAF. The interfacial coefficient \( f(h) \) determines the specific profile of these minima and the energy barrier between them [44,45]. The switch between the global and metastable minima with changing temperature is probably triggered by the \( \Delta G_{\text{vol}} \cdot h \) term, which increases with a reduction of temperature in the subsolidus regime (Fig. 8). This analysis implies a first-order adsorption transition from monolayer-to-multilayer coverage, the existence of which is further supported by the observations of the hysteresis loops in the thickness vs temperature curves and the relatively abrupt transitions in film thicknesses in Fig. 7a and b.

A first-order wetting (adsorption) transition that occurs when the phase doing the wetting is not yet stable is called a prewetting transition [21]. This prewetting transition, originally proposed in the Cahn critical point wetting model for binary de-mixed liquids [46], has been observed in organic systems [47,48] and in the Pb–Ga liquid metal system [49,50]. In the present case, the transition from
low- to high-adsorption structures is coupled with an interfacial disordering transition, occurring at a subsolidus temperature, to permit an analogy to premelting in unary systems [20]. Thus, it is conceptually useful to interpret this surface transition as a coupled prewetting and premelting [20] transition, which leads to the formation of quasi-liquid surficial films with a high level of adsorption. Further discussions of the phenomenological similarities among equilibrium-thickness SAF and IGF, prewetting, premelting, and frustrated-complete wetting can be found in recent review articles [3,13].

A surface transition can be modeled via a diffuse-interface theory [19], which combines the Cahn critical point wetting model for surfaces in binary de-mixed liquids [46] and the Tang–Carter–Cannon model for GB (IGF) in binary alloys [22]. In particular, the energy barrier between the two minima in the free energy vs film thickness shown in Fig. 10 is probably related to the high volumetric free energy for the intermediate state between a bulk (binary) liquid and a bulk crystal [19]. This energy barrier is the possible origin of the first-order transition. The hysteresis and bimodal thickness distributions shown in Figs. 7 and 8 are probably related to the nucleation of small crystallites in surficial films (when the mass transport rate is limited), and such crystallites can be seen in Fig. 1b.

Recent discoveries of multiple GB complexities (phases) with possible GB transitions in doped Al2O3 by Dillon et al. [5,6] resolves an outstanding scientific problem of the abnormal grain growth mechanism. Indications of GB prewetting/premelting transitions have also been found for Cu–Bi [51–56] and Fe–Si–Zn (where the primary phases are underlined) [53,57–60].

4. Concluding remarks

Vanadia-based, equilibrium-thickness, surficial films were observed on TiO2 anatase (101) and (001) facets and curved surfaces in the V2O5–TiO2 binary system, and in six ternary oxide systems. Co-doping can be used to tune the equilibrium thickness of these films. The average measured thickness was found to increase with the addition of P, decrease with the addition of Mo, W and Nb, and remain stable with the addition of K and Na. Co-doping can also be used to tailor the film thickness distribution, anisotropy and surface coverage. Furthermore, both film appearance and thickness can be tuned by changing equilibration temperature (and, presumably, any other intensive thermodynamic variables).

Observations of abrupt transitions in film thicknesses, hysteresis loops in the thickness vs temperature curves, and further analysis of bimodal thickness distributions and their evolution suggest the possible existence of a first-order monolayer-to-multilayer adsorption transition. Consequently, these SAF were interpreted as quasi-liquid films or multilayer adsorbates formed from coupled premelting and prewetting transitions in a generalized Cahn critical point wetting model. Since first-order surface or GB transitions can cause abrupt changes in transport kinetics (e.g., surface/GB diffusivity, GB mobility, surface reaction/growth rates) and mechanical/physical properties (e.g., creep and surface friction) [3], confirming and comprehending such transitions are important for controlling microstructural evolution, growth of nanocrystals, and properties of the resultant materials.

More than 850 independent films were observed. The measurements of film appearance and thickness as a function of various controlled parameters provide an important dataset for elucidating the general formation mechanisms of both SAF and IGF.

Further experiments to characterize the catalytic properties of these surficial films are in progress. In general, catalytic properties are probably sensitive to the detailed structure of the overlayers (i.e., monolayers or nanoscale surficial films) [61]. The specific co-doping effects probably depend on the interaction of these respective co-dopants with the dangling V=O bonds. Furthermore, the co-doping effects are expected to differ for different catalytic reactions. For selective catalytic reduction of NOx by NH3, MoO3, WO3 and Nb2O5 co-dopants are known as "promoters", while K2O and Na2O co-dopants are known to have poisoning effects [62,63]. It is also known that the addition of P2O5 has little effect on the catalytic activity for butadiene oxidation [62]. While there are probably no general conclusions on whether the formation of nanometer-thick surficial films and the addition of co-dopants are beneficial or detrimental on the resultant catalytic properties, the ability to tailor the structure and composition of these films via controlling thermodynamic variables offers a new dimension for tailoring supported catalysts at the nanoscale.

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